Name _____

<u>Target 7-1</u>: I can describe transformations, domain and range, and graph exponential and logarithmic functions.

1. $y = -4\left(\frac{1}{2}\right)^{x+2}$	2. $y = \frac{1}{5}(2)^{x-1}$
Parent function:	Parent function:
<i>a</i> = meaning	a = meaning
<i>h</i> = meaning	h = meaning
<i>k</i> = meaning	k = meaning
Domain:	Domain:
Range:	Range:
$3. y = 2\left(\frac{1}{5}\right)^x - 1$	4. $y = \frac{1}{2}(3)^{x+4} - 5$
Parent function:	Parent function:
a = meaning	a = meaning
h = meaning	h = meaning
<i>k</i> = meaning	k = meaning
Domain:	Domain:
Range:	Range:
5. $y = 3 \log_2 x + 1$	6. $y = 2 \log_{\frac{1}{4}}(x-3) + 2$
Parent function:	Parent function:
a = meaning	a = meaning
h = meaning	h = meaning
k = meaning	<i>k</i> = meaning
Domain:	Domain:
Range:	Range:
7. $y = \frac{1}{2}\log_8(x+1) - 2$	8. $y = -2\log_2(x-4) + 3$
Parent function:	Parent function:
a = meaning	a = meaning
h = meaning	h = meaning
k = meaning	k = meaning
Domain:	Domain:
Range:	Range:

Graphs for T7-1



T7-2 RETAKE WS Solving & Writing Exponential Equations

Solve each equation.

1.
$$25^{x+5} = 125^{x-3}$$
 2. $\left(\frac{1}{27}\right)^{\frac{1}{3}x-5} = 9^{x-3}$

3.
$$11^{x-4} = 121^{x+28}$$

4. $\left(\frac{1}{6}\right)^{2x+2} = 216^{x-1}$

5.
$$\left(\frac{1}{2}\right)^{x-3} = 16^{3x+1}$$
 6. $3^{6x-2} = \left(\frac{1}{9}\right)^{x+1}$

Write an exponential function in the form $y = ab^x$ for the graph that passes through the given points.

7. (0, 5) and (4, 3125) **8.** (0, 8) and (4, 2048) **9.** $\left(0, \frac{3}{4}\right)$ and (2, 36.75)

10.
$$(0, -0.2)$$
 and $(-3, -3.125)$
11. $(0, 15)$ and $\left(2, \frac{15}{16}\right)$
12. $(0, 0.7)$ and $\left(\frac{1}{2}, 3.5\right)$

Solve each equation.

13.
$$20.400 = \left(\frac{1}{20}\right)^{7x+11}$$
 14. $10^{4x+8} = 1000^x$ **15.** $\left(\frac{1}{16}\right)^{3x-4} = 64^{x-1}$

16.
$$\left(\frac{1}{8}\right)^{x-6} = 4^{4x+5}$$
 17. $\left(\frac{1}{36}\right)^{x+8} = 6^x \cdot 216^{x-3}$ **18.** $128^{x+3} = \left(\frac{1}{1024}\right)^{2x}$

19. At time *t*, there are 216^{t+18} bacteria of type A and 36^{2t+8} bacteria of type B organisms in a sample. When will the number of each type of bacteria be equal?

T7-3 RETAKE WS Solving Logarithmic Equations

Side 1 – w/o properties

Solve each equation.

- **1.** $3x = \log_6 216$ **2.** $x 4 = \log_3 243$ **3.** $\log_4 (4x 20) = 5$
- **4.** $\log_9 (3-x) = \log_9 (5x-15)$ **5.** $\log_{81} (x+20) = \log_{81} (6x)$ **6.** $\log_9 (3x^2) = \log_9 (2x+1)$
- **7.** $\log_4 (x-1) = \log_4 (12)$ **8.** $\log_7 (5-x) = \log_7 (5)$ **9.** $\log_x (5x) = 2$

Solve each equation.

- **10.** $\log_5 (-3x) = 1$ **11.** $\log_6 x = \log_6 (4 x)$
- **12.** $\log_{10} (x-3) = 2$ **13.** $\log_2 (x-5) = \log_2 (3)$
- **14.** $\log_7 (8x + 5) = \log_7 (6x 18)$ **15.** $\log_9 (3x 3) = 1.5$
- **16.** $\log_{10} (2x 2) = \log_{10} (7 x)$ **17.** $\log_9 (x 1) = \log_9 (2x)$
- **18.** $\log_{16} x \ge 0.5$ **19.** $\log_3 \left(\frac{x-3}{4}+5\right) > \log_3 (x+2)$
- **20.** $\log_5 (3x) = \log_5 (2x 1)$ **21.** $\log_3 (7 x) = \log_3 (x + 19)$

T7-3 RETAKE WS Solving Logarithmic Equations

Solve each equation. Check your solutions.

1.
$$\log_7 n = \frac{2}{3} \log_7 8$$
 2. $\log_{10} u = \frac{3}{2} \log_{10} 4$

3. $\log_6 x + \log_6 5 = \log_6 45$ **4.** $\log_8 32 - \log_8 w = \log_8 4$

5.
$$\log_9 (3u + 14) - \log_9 5 = \log_9 2u$$

6. $4 \log_2 x + \log_2 5 = \log_2 405$

7. $\log_3 y = -\log_3 16 + \frac{1}{3}\log_3 64$ **8.** $\log_2 d = 5\log_2 2 - \log_2 8$

9. $\log_{10} (3m-5) + \log_{10} m = \log_{10} 2$ **10.** $\log_{10} (b+3) + \log_{10} b = \log_{10} 4$

11. $\log_8 (t+10) - \log_8 (t-1) = \log_8 12$ **12.** $\log_3 (a+3) + \log_3 (a+2) = \log_3 6$

13. $\log_{10} (r+4) - \log_{10} r = \log_{10} (r+1)$ **14.** $\log_4 (x^2-4) - \log_4 (x+2) = \log_4 1$

15. $\log_{10} 4 + \log_{10} w = 2$ **16.** $\log_8 (n-3) + \log_8 (n+4) = 1$

17.
$$3 \log_5 (x^2 + 9) - 6 = 0$$
 18. $\log_{16} (9x + 5) - \log_{16} (x^2 - 1) = \frac{1}{2}$

19. $\log_6 (2x-5) + 1 = \log_6 (7x+10)$ **20.** $\log_2 (5y+2) - 1 = \log_2 (1-2y)$

T7-4 RETAKE WORKSHEET

Per

- 1. Ten grams of Carbon 14 is stored in a container. The amount C (in grams) of Carbon 14 present after t years can be modeled by $C = 10(0.99987)^t$. How much is present after 1000 years?
- 2. You deposit \$2000 in an account that earns 5% annual interest. <u>Write a function</u> for each of the following frequencies. Then determine the balance after 2 years if the interest is compounded with the given frequency.

a. annually	b. quarterly	c. monthly
Function:	Function:	Function:
Balance:	Balance:	Balance:

- 3. A customer purchases a television for \$800 using a credit card. The interest is charged on an unpaid balance at a rate of 18% per year compounded monthly. If the customer makes no payment for one year, how much is owed at the end of the year?
- 4. A diamond ring was purchased twenty years ago for \$500. The value of the ring increases by 8% each year. What is the value of the ring today?
- 5. In 1990 the tuition at a private college was \$15000. During the next 9 years, tuition increased by about 7.2% each year.
 - a. Write a model giving the cost C of tuition at the college t years after 1990
 - b. About what year will the tuition be \$20,000?
 - c. If this trend continues what will the tuition be in 2010?

- 6. The number of newly reported cases of tuberculosis in the US in 1991 was 28,500. In 1996 it went down to 22,841. The decrease in cases models exponential decay. Write a function to model this situation where t represents the number of years since 1991.
 - a. Identify the initial amount, decay factor and annual percent decrease.
 - b. In what year was the number of newly reported cases in US approximately 25,000?
 - c. When will the number of newly reported cases be about 16,000?
 - d. Estimate the number of newly reported cases in 2005.
- 7. A tool & die business purchased a piece of equipment of \$250,000. The value of the equipment depreciates at a rate of 12% each year.
 - a. Write an exponential decay model for the value of equipment.
 - b. What is the value of equipment after 5 years?
 - c. Approximately when the equipment will have a value of \$70,000?
- 8. A house was purchased for \$90,000 in 1995. If the value of the home increases 5% per year, what is it worth in the year 2020?

Function:_____

Worth in 2020: _____

- 9. You deposit \$1000 in an account that earns 2.5% annual interest. Find the balance after 3 years if the interest compounds with the given frequency.
 - a. **monthly** Function: Balance:

b. **daily** Function: Balance: