

## Stick Quiz

- 1** Write a quadratic equation with the roots  $-1$  and  $\frac{3}{4}$  in the standard form.

$$4x^2 + x - 3 = 0$$

- 2** Solve  $3s^2 - 11s - 4 = 0$  by factoring.

$$-\frac{1}{3}, 4$$

- 3** Solve  $2x^2 + 5x + 3 = 0$  by factoring.

$$-\frac{3}{2}, -1$$

$$\begin{array}{l}
 x = -1 \quad 4x = \frac{3}{4} \\
 \begin{array}{cc}
 +1 & +1 \\
 \hline
 (x+1) = 0 & (4x-3) = 0 \\
 \hline
 (x+1)(4x-3) = 0
 \end{array}
 \end{array}$$

Solve  $3s^2 - 11s - 4 = 0$  by factoring.

$$3x^2 - 11x - 4 = 0$$

$$(3x^2 - 12x) + (1x - 4) = 0$$

$$3x(x - 4) + 1(x - 4) = 0$$

$$(x - 4)(3x + 1) = 0$$

$$x - 4 = 0 \quad 3x + 1 = 0$$

$$x = 4 \quad -1$$

$$\frac{3x}{3} = \frac{-1}{3}$$

$$\begin{array}{r|l} -12 & -1 \\ \hline 1:12 & 1x + -12x \\ 2:6 & \\ 3:4 & \end{array}$$

$$x = 4, -\frac{1}{3}$$

? ? ? ?

# Questions

? ? ? ?

# On

? ? ? ?

# Homework

? ? ? ?

? ? ? ?

? ? ? ?

# LESSON 4-4 Complex Numbers

## Part 1

I can... perform algebraic operations to complex numbers.

Solve for x.

$$x^2 + 64 = 0$$

$$\sqrt{x^2} = \sqrt{-64}$$

$$x = \pm\sqrt{-64}$$

$$\begin{array}{r|l} 64 & 0 \\ 8 \cdot 8 & \cancel{16} \\ -8 \cdot -8 & \cancel{-16} \end{array}$$

**Problem! We can't find the square root of a negative number!**

# Oh wait... We can!!!

## Introducing: Imaginary Numbers!

$$i = \sqrt{-1}$$

$$i^2 = (\sqrt{-1})^2 = -1$$

$$i^3 = (\sqrt{-1})^3 = (\sqrt{-1})(\sqrt{-1})(\sqrt{-1}) = -1 \cdot i = -i$$

$$i^4 = (\sqrt{-1})^4 = (\sqrt{-1})^2 (\sqrt{-1})^2 = -1 \cdot -1 = 1$$

$$\sqrt{-1} \quad \boxed{\begin{array}{l} i = \sqrt{-1} \\ i^2 = -1 \\ i^3 = -i \\ i^4 = 1 \end{array}} \quad i$$

So... What is  $\sqrt{-4}$ ?

$$\begin{aligned} \sqrt{-4} &= \sqrt{-1 \cdot 4} \\ &= \sqrt{-1} \cdot \sqrt{4} \\ &= i \cdot 2 \\ &= 2i \end{aligned}$$

$$\sqrt{10} = \sqrt{2 \cdot 5} = \sqrt{2} \cdot \sqrt{5}$$

$$\sqrt{6} \cdot \sqrt{3} = \sqrt{18} =$$

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$$\sqrt{100} = 10$$

$$\sqrt{-100} = 10i$$

$$\sqrt{49}$$

$$\sqrt{-49}$$

$$\sqrt{36}$$

$$\sqrt{-36}$$

$$\sqrt{25}$$

$$\sqrt{-25}$$

$$\sqrt{-5} = \sqrt{-1 \cdot 5} \quad \sqrt{-1} \sqrt{5} = i\sqrt{5}$$
$$i\sqrt{5}$$

$$\sqrt{-7}$$
$$\sqrt{-13}$$
$$\sqrt{-15}$$

**Back to our problem...**

$$x^2 + 64 = 0$$

$$x = -8i$$

$$x = \pm \sqrt{-64}$$

$$x = 8i$$

$$x = \pm i\sqrt{64}$$

## Simplifying Radicals

**Perfect Squares!**

1.  $\sqrt{144} = \underline{12}$

2.  $\sqrt{100} = \underline{10}$

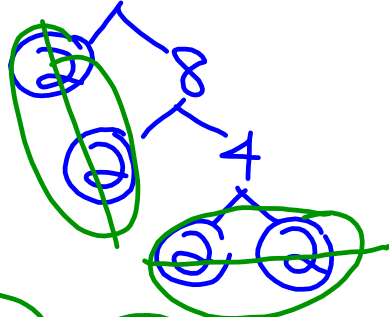
Find a Biggest Perfect Square that divides into the number under the radical.

3.  $\sqrt{32} = \underline{\hspace{2cm}}$

4.  $\sqrt{18} = \underline{\hspace{2cm}}$

$$\sqrt{32} = 2 \cdot 2 \sqrt{2} = 4\sqrt{2}$$

$$\sqrt{2 \cdot 16} = \sqrt{2} \sqrt{16} = 4\sqrt{2}$$



$$\sqrt{18}$$

$$\sqrt{2 \cdot 2 \cdot 2 \cdot 2 \cdot 2}$$

6. Simplify

$$\sqrt{-2} \cdot \sqrt{-6}$$

$$i\sqrt{2} \cdot i\sqrt{6}$$

$$i^2 \sqrt{12} = 2(\sqrt{3}) = -2\sqrt{3}$$

$$\sqrt{-3} \cdot \sqrt{-6}$$

First take out i

Second Squish together

Simplify

$$\begin{array}{r} \sqrt{12} \\ \hline \sqrt{3 \cdot 4} \\ 2\sqrt{3} \end{array}$$

$$\sqrt{-3} \cdot \sqrt{-6}$$

$$i\sqrt{3} \cdot i\sqrt{6}$$

$$i^2 \sqrt{18} = i^2 \sqrt{2} \sqrt{9} = \cancel{3} \cdot 3\sqrt{2}$$

$$\begin{array}{c} \textcircled{2} \textcircled{9} \\ \textcircled{3} \textcircled{3} \end{array}$$

$$-3\sqrt{2}$$



$$\sqrt{100}$$

$$\sqrt{49}$$

$$\sqrt{121}$$

$$\sqrt{-100}$$

$$\sqrt{-49}$$

$$\sqrt{-36}$$

$$\sqrt{-5}$$

$$\sqrt{-10}$$

You Try!      White Boards

7. **Simplify**  $\sqrt{-50}$ .

$$5i\sqrt{2}$$

8. **Simplify**  $\sqrt{-45}$ .

$$3i\sqrt{5}$$

9. Simplify  $\sqrt{-6} \cdot \sqrt{-8}$

Solve

9.  $4x^2 + 4 = 0$

10.  $2x^2 + 10 = 0$

You Try! On the White Boards!!!!

Solve.

11.  $2x^2 + 50 = 0$

12.  $6x^2 + 108 = 0$

$$\begin{aligned} & -108 \quad -108 \\ \frac{6x^2}{6} &= \frac{-108}{6} \\ \sqrt{x^2} &= \sqrt{-18} \\ x &= \pm \sqrt{-18} \end{aligned}$$

**Simplify:** White Boards!!!!

$4x + 2x$

$3x - 5x$

$4i + 2i$

$3i - 5i$

## Complex Number

$$a + bi$$

\*\* Add reals \*\*\* Add Imaginary\*\*

Adding Complex Numbers:

$$(2 - 4i) + (3 + 5i) = 5 + i$$

$$(-3 + 6i) + (7 - 4i)$$

Subtracting Complex Numbers:

$$(2 - 4i) - (3 + 5i)$$

$$2 - 4i - 3 - 5i = -1 - 9i$$

$$(-3 + 6i) - (7 - 4i)$$

You Try! Simplify the expression.

White Boards!!!

13.  $(3 + 5i) + (2 - 4i)$



15.  $(4 - 6i) - (3 - 7i)$



## Multiplying/Dividing Complex Numbers

Next class!

Homework 4.4

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#18-23, 26-29, 36-41, 48,

49, 51, 52, 66

**Different than your Stamp Sheet!**